

**Problem 1 [Poston Prob. 1.1]**

Identify the decay products of the following nuclides given their mode of decay:

${}_{38}^{90}\text{Sr}(\beta)$ ,  ${}_{92}^{238}\text{U}(\alpha)$ ,  ${}_{61}^{147}\text{Pm}(\beta)$ ,  ${}_{35}^{78}\text{Br}(\beta^+)$ ,  ${}_{36}^{79}\text{Kr}(\text{EC})$ ,  ${}_{86}^{222}\text{Rn}(\alpha)$ ,  ${}_{43}^{99m}\text{Tc}(\gamma)$ ,  ${}_{98}^{252}\text{Cf}(\text{SF})$

**Problem 2 [Poston Prob. 1.10]**

${}^{131}\text{I}$  has a radioactive half-life of 8 days and a liver excretion half-time of 55 min. Plot the effective decay rate for 1 mCi of labeled material in the liver.

**Problem 3 [Poston Prob. 1.11]**

${}^{64}\text{Cu}$  decays by positron ( $\beta^+$ ), internal conversion and electrons ( $\beta^-$ ). Identify the decay products and the amounts accumulating over the life ( $7T_{1/2}$ ) of the source.

$\text{Cu}$  ( $T_{1/2}=12.8$  h)

Branching ratios are:  $\beta^-$  38%,  $\beta^+$  19%, CE 43%.

**Problem 4 [Poston Prob. 1.13]**

A geiger counter has a background count of 60 cpm. It is placed in a uniform  $\gamma$  radiation field. If the detection efficiency is 3%, calculate the minimum intensity required for a net count rate of five times the background.

**Problem 5 [Poston Prob. 1.16]**

Determine the relative intensities of the

- 1.29 and 1.098 MeV  $\gamma$ -ray emissions in the decay of  ${}^{59}\text{Fe}$ ,
- the 0.177 and 0.284 MeV lines of  ${}^{131}\text{I}$ .

**Problem 6 [Poston Prob. 1.17]**

Natural antimony consists of  ${}^{121}\text{Sb}$  (57.25%,  $\sigma_{n\gamma} = 6b$ ) and  ${}^{123}\text{Sb}$  (42.75%,  $\sigma_{n\gamma} = 4b$ ). Neutron activation produces  ${}^{122}\text{Sb}$  ( $T_{1/2} = 2.8$  days) and  ${}^{124}\text{Sb}$  ( $T_{1/2} = 60$  days).

Calculate the activities produced if a 5-g sample of antimony is exposed in a neutron flux of  $10^{13}$  n/cm<sup>2</sup>-sec for

- 2 hours

b) 2 days

c) 1 year

Determine in each case how long the source would have to cool down in each case for the  $^{122}\text{Sb}$  activity to constitute less than 10% of the total activity.

### Problem 7 [Poston Prob. 1.2]

A given accelerator produces neutrons by the (d,n) reaction on beryllium. If the beam current is 50 milliamps and the conversion efficiency is 1%, calculate the neutron production rate.

### Problem 8 [Poston Prob. 1.3]

A certain  $^{238}\text{Pu}$  source has an activity of 50 millicuries. If all the alpha particles are self absorbed in the source material, calculate the heat production (alpha energy = 5.5 MeV)

### Problem 9 [Poston Prob. 1.4]

In the previous question, estimate the amount of helium generated in the source in one year. If the source capsule has internal dimensions of 5 mm diameter by 2 mm thick and 5% void space, calculate the helium pressure after one year.

### Problem 10 [Poston Prob. 1.5]

A 10 MBq  $^{60}\text{Co}$  source consists of a thin wire 2 mm in length. Calculate the gamma-ray intensity at 30 cm and 2 m distance from that source.

### Problem 11 [Poston Prob. 1.6]

Calculate the mass needed to produce an activity of 10 mCi of the following nuclides:  $^{226}\text{Ra}$ ,  $^{131}\text{I}$ ,  $^{65}\text{Zn}$ ,  $^{24}\text{Na}$

### Problem 12 [Poston Prob. 1.7]

Calculate the amount of  $^{99m}\text{Tc}$  ( $T_{1/2}=6$  hours) that is present in a 50 mCi  $^{99}\text{Mo}$  ( $T_{1/2}=67$  hours) a) 6 hours, b) 12 hours, c) 30 hr, d) 67 hours, e) 150 hours after the molybdenum source was freshly prepared.

**Problem 13 [Poston Prob. 1.8]**

A 100-mg silver foil is irradiated in a neutron flux of  $10^{13}$  neutrons/( $\text{cm}^2 \cdot \text{sec}$ ).  $^{109}\text{Ag}$  has an abundance of 48.17% and cross sections of 4b and 88b, respectively, to produce  $^{110}\text{Ag}$  ( $T_{1/2}=253$  days) and  $^{110m}\text{Ag}$  ( $T_{1/2}=24\text{sec}$ ). Calculate the activity of this foil after 5-min exposure and after 3-min and 3-hr cooling times.

**Problem 14 [Turner Prob. 3.12]**

- (a) Calculate the energy released by the alpha decay of  $^{222}_{86}\text{Rn}$
- (b) Calculate the energy of the alpha particle
- (c) What is the energy of the recoil polonium atom?

**Problem 15 [Turner Prob. 3.15]**

The Q value for alpha decay of  $^{239}_{94}\text{Pu}$  is 5.25 MeV. Given the masses of the  $^{239}\text{Pu}$  and  $^4\text{He}$  atoms, 239.052174 AMU and 4.002603 AMU, calculate the mass of the  $^{235}_{92}\text{U}$  atom in AMU.

**Problem 16 [Turner Prob. 3.17]**

- (a) Calculate the energy released in the beta decay of  $^{32}_{15}\text{P}$ .
- (b) If a beta particle has 650 keV, how much energy does the antineutrino have?

**Problem 17 [Turner Prob. 3.20]**

A  $^{108}_{49}\text{In}$  source emits a 633 keV gamma photon and a 606 keV internal conversion electron from the K shell. What is the binding energy of the electron in the K shell?

**Problem 18 [Turner Prob. 3.24]**

Nuclide A decays into nuclide B by  $\beta^+$  emission (24%) or by electron capture (76%). The major radiations, energies (in MeV), and frequencies per disintegration are:

$\beta^+$ : 1.62 max (16%), 0.98 max (8%)

$\gamma$ : 1.51 (47%), 0.64(55%), 0.511(48%,  $\gamma^\pm$ )

Daughter X rays

$e^-$ : 0.614

- (a) Draw the nuclear decay scheme, labeling type of decay, percentages and energies
- (b) What leads to the emission of the daughter X rays?

**Problem 19 [Turner Prob. 3.27]**

A parent nuclide decays by beta-particle emission into stable daughter. The major radiations, energies (in MeV), and frequencies per disintegration are:

$$\beta^-: 3.92 \text{ max (7\%), 3.10 max (8\%), 1.60 max (88\%)}$$

$$\gamma: 2.32 (34\%), 1.50(54\%), 0.820(49\%)$$

$$e^-: 0.818, 0.805$$

- (a) Draw the nuclear decay scheme.
- (b) What is the maximum energy that the antineutrino can receive in this decay?
- (c) What is the value of the internal conversion coefficient?
- (d) Estimate the L-shell electron binding energy of the daughter nuclide.
- (e) Would daughter X rays be expected also? Why or why not?

**Problem 20 [Turner Prob. 3.29]**

Refer to the decay scheme of  $^{137}_{55}\text{Cs}$ . The binding energies of the K- and L-shell electrons of the daughter  $^{137}_{56}\text{Ba}$  atom are 38 keV and 6 keV.

- (a) What are the energies of the internal conversion electrons ejected from these shells?
- (b) What is the wavelength of the  $K_\alpha$  X ray emitted when an L-shell electron makes a transition to the K-shell?
- (c) What is the value of the internal conversion coefficient?

**Problem 21 [Turner Problem 3.3]**

What minimum energy would an alpha particle need in order to react with a  $^{238}\text{U}$  nucleus?

**Problem 22 [Turner Prob. 3.30]**

- (a) Calculate the Q value for the K orbital electron capture by the  $^{37}_{18}\text{Ar}$  nucleus, neglecting the electron binding energy.
- (b) Repeat (a), including the binding energy, 3.20 keV, of the K-shell electron in argon.
- (c) What becomes of the energy released as a result of this reaction?

**Problem 23** [Turner Prob. 3.31]

What is the maximum possible positron energy in the decay of  ${}^{35}_{18}\text{Ar}$ ?

**Problem 24** [Turner Prob. 3.36]

The isotope  ${}^{126}_{53}\text{I}$  can decay by EC,  $\beta^-$  and  $\beta^+$  transitions.

- Calculate the Q values for the three modes of decay to the ground states of the daughter nuclei.
- Draw the decay scheme.
- What kind of radiation can one expect from a  ${}^{126}\text{I}$  source?

**Problem 25** [Turner Prob. 3.5]

Calculate the total binding energy of the alpha particle.

**Problem 26** [Turner Prob. 3.8]

Calculate the binding energy per nucleon for the nuclide  ${}^{40}_{19}\text{K}$

**Problem 27** [Turner Prob. 4-10]

How many grams of  ${}^{32}\text{P}$  are there in a 5 *mCi* source?

**Problem 28** [Turner Prob. 4-12]

An encapsulated  ${}^{210}\text{Po}$  radioisotope was used as a heat source, in which an implanted thermocouple junction converts heat into electricity with an efficiency of 15% to power a small transmitter for an early space probe.

- How many curies of  ${}^{210}\text{Po}$  are needed at launch time if the transmitter is to be supplied with 100 W of electricity 1 year after launch.
- Calculate the number of grams of  ${}^{210}\text{Po}$  needed.
- If the transmitter shuts off when the electrical power to it falls below 1 W, how long can it be expected to operate after launch?

**Problem 29** [Turner Prob. 4-13]

The Cassini spacecraft went into orbit about the planet Saturn in July 2004 after a nearly seven-year journey from Earth. On-board electrical systems were powered by heat from three

radioisotope thermoelectric generators, which together utilized a total of 32.7 kg of  $^{238}\text{Pu}$ , encapsulated as  $\text{PuO}_2$ . The isotope has a half-life of 86.4 years and emits an alpha particle with an average energy of 5.49 MeV. The daughter  $^{234}\text{U}$  has a half-life of  $2.47 \times 10^5$  years.

- (a) Calculate the specific thermal power generation rate of  $^{238}\text{Pu}$  in W/g.  
(b) How much total thermal power is generated in the spacecraft?

### Problem 30 [Turner Prob. 4-14]

A 0.2 g sample of  $^{85}\text{Kr}$  gas, which decays into stable  $^{85}\text{Rb}$ , is accidentally broken and escapes inside a sealed warehouse measuring  $40 \times 30$  m. What is the specific activity of the air inside?

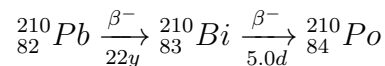
### Problem 31 [Turner Prob. 4-15]

A 6.2 mg sample of  $^{90}\text{Sr}$  is in secular equilibrium with its daughter  $^{90}\text{Y}$ .

- (a) How many Bq of  $^{90}\text{Sr}$  are present? (b) How many Bq of  $^{90}\text{Y}$  are present? (c) What is the mass of  $^{90}\text{Y}$  present? (d) What will be the activity of the  $^{90}\text{Y}$  be after 100 years?

### Problem 32 [Turner Prob. 4-17]

Consider the following  $\beta^-$  nuclide decay chain with the half-lives indicated:



A sample contains 30 MBq of  $^{210}\text{Pb}$  and 15 MBq  $^{210}\text{Bi}$  at time  $t=0$ .

- (a) Calculate the activity of  $^{210}\text{Bi}$  at time  $t=10\text{d}$ .  
(b) If the sample was originally pure  $^{210}\text{Pb}$ , then how old is it at time  $t=0$ ?

### Problem 33 [Turner Prob. 4-19]

$^{59}\text{Fe}$  has a half-life of 45.33 d.

- (a) What is the mean life of a  $^{59}\text{Fe}$  atom?  
(b) What is the specific activity of a  $^{59}\text{Fe}$ .  
(c) How many atoms are there in a 10 *mCi* source of  $^{59}\text{Fe}$ ?

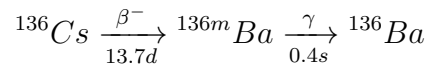
### Problem 34 [Turner Prob. 4-20]

At time  $t=0$  a sample consists of 2 *Ci* of  $^{90}\text{Sr}$  and 8 *Ci* of  $^{90}\text{Y}$ .

- (a) What will be the activity of  $^{90}\text{Y}$  be in the sample after 100 h?  
(b) At what time will the  $^{90}\text{Y}$  activity be equal to 3 *Ci*?

**Problem 35** [Turner Prob. 4-21]

$^{136}\text{Cs}$  decays into  $^{136}\text{Ba}$  as follows:



- Calculate the decay constant of  $^{136}\text{Cs}$ .
- Calculate the specific activity of  $^{136}\text{Cs}$
- Starting with a pure  $10^{10}$  Bq sample of  $^{136}\text{Cs}$  at time  $t=0$ , how many atoms of  $^{136m}\text{Ba}$  decay between time  $t_1=13.7\text{d}$  (exactly) and time  $t_2=13.7\text{d}+5\text{s}$ ?

**Problem 36** [Turner Prob. 4-24]

A 40 mg sample of pure  $^{226}\text{Ra}$  is encapsulated.

- How long will it take for the activity of  $^{222}\text{Rn}$  to build up to 10 *mCi*?
- What will be the activity of  $^{222}\text{Rn}$  after 2 years?
- What will be the activity of  $^{222}\text{Rn}$  after 1000 years?
- What is the ratio of the specific activity  $^{222}\text{Rn}$  to that of  $^{226}\text{Ra}$ ?

**Problem 37** [Turner Prob. 4-28]

The average mass of potassium in the human body is about 140 g. Estimate the average activity of  $^{40}\text{K}$  in the body.

**Problem 38** [Turner Prob. 4.3]

The activity of a radioisotope is found to decrease by 30% in one week. What are the values of its:

- decay constant
- half-life
- mean life?

**Problem 39** [Turner Prob. 4.5]

The isotope  $^{132}\text{I}$  decays by  $\beta^-$  emission into stable  $^{132}\text{Xe}$  with a half-life of 2.3 h.

- How long it will take for  $\frac{7}{8}$  of the original  $^{132}\text{I}$  atoms to decay?
- How long it will take for a sample of  $^{132}\text{I}$  to lose 95% of its activity?

**Problem 40** [Turner Prob. 4-6]

A very old specimen of wood contained  $10^{12}$  atoms of  $^{14}\text{C}$  in 1986.

- (a) How many  $^{14}\text{C}$  atoms did it contain in the year 9474 BC?
- (b) How many  $^{14}\text{C}$  atoms did it contain in 1986 BC?

**Problem 41** [Turner Prob. 4-7]

A radioactive sample consists of a mixture of  $^{35}\text{S}$  and  $^{32}\text{P}$ . Initially, 5% of the activity is due to the  $^{35}\text{S}$  and 95% to the  $^{32}\text{P}$ . At what subsequent time will the activities of the two nuclides in the sample be equal?

**Problem 42** [June 2013]

In an experiment designed to measure the total neutron cross section of 10 MeV with lead, the neutron flux after passing a 1 cm thick rod is found to be 84.5% of its initial value. If the atomic weight of lead is 207.21 g/mol and its density is  $11.3 \text{ g/cm}^3$

- a) Calculate the total effective cross-section (in barns)
- b) Calculate also the macroscopic cross section